## Chapter 7: Similarity

## I Can

- Prove if triangles are similar with (AA, SSS and SAS)
- Use triangle similarity to solve problems


## Proving Similarity

There are several ways to prove certain triangles are similar. The following postulates will be used in proofs just as SSS, SAS, ASA, HL, and AAS were used to prove triangles congruent.

| Postulate 7-3-1 Angle-Angle (AA) Similarity |  |  |  |
| :--- | :---: | :---: | :---: |
| POSTULATE HYPOTHESIS CONCLUSION  <br> If two angles of one triangle <br> are congruent to two angles <br> of another triangle, then the <br> triangles are similar.    |  |  |  |

Proving Similarity

| THEOREM | HYPOTHESIS | CONCLUSION |
| :---: | :---: | :---: |
| If the three sides of one triangle are proportional to the three corresponding sides of another triangle, then the triangles are similar. |  | $\triangle A B C \sim \triangle D E F$ |

Theorem 7-3-3 (Side-Angle-Side (SAS) Similarity

| THEOREM | HYPOTHESIS | CONCLUSION |  |
| :--- | :--- | :--- | :--- |
| If two sides of one triangle <br> are proportional to two <br> sides of another triangle <br> and their included angles <br> are congruent, then the <br> triangles are similar. | $B$ |  |  |

## Example

## Explain why the triangles

 are similar and write a similarity statement.

## Example

## Verify that the triangles are similar.

## $\triangle P Q R$ and $\triangle S T U$



## Example



## Example

Explain why $\triangle A B E \sim \triangle A C D$, and then find $C D$.


## Properties

| Properties of Similarity |
| :--- |
| Reflexive Property of Similarity |
| $\triangle A B C \sim \triangle A B C$ (Reflex. Prop. of $\sim$ ) |
| Symmetric Property of Similarity |
| If $\triangle A B C \sim \triangle D E F$, then $\triangle D E F \sim \triangle A B C$. (Sym. Prop. of $\sim$ ) |
| Transitive Property of Similarity |
| If $\triangle A B C \sim \triangle D E F$ and $\triangle D E F \sim \triangle X Y Z$, then $\triangle A B C \sim \triangle X Y Z$. |
| (Trans. Prop. of $\sim$ ) |

## PROOFS!!

Given: $\mathbf{3 U T}=\mathbf{5 R T}$ and $\mathbf{3 V T}=\mathbf{5 S T}$
Prove: $\triangle U V T \sim \Delta R S T$


## I Can

- Prove if triangles are similar with (AA, SSS and SAS)
- Use triangle similarity to solve problems

