Chapter 7: Similarity

SECTION 3: TRIANGLE SIMILARITY (AA, SSS, SAS)

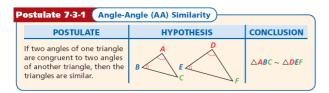
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Proving Similarity

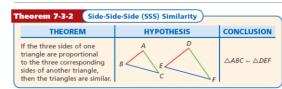
There are several ways to prove certain triangles are similar. The following postulates will be used in proofs just as SSS, SAS, ASA, HL, and AAS were used to prove triangles congruent.



I Can

- ☐ Prove if triangles are similar with (AA, SSS and SAS)
- ☐ Use triangle similarity to solve problems

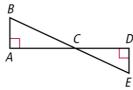
Proving Similarity



Theorem 7-3-3 Side-Angle-Side (SAS) Similarity			
THEOREM		HYPOTHESIS	CONCLUSION
If two sides of one triangle are proportional to two sides of another triangle and their included angles are congruent, then the triangles are similar.		$B \xrightarrow{A} E \xrightarrow{D} E$ $\angle B \cong \angle E$	△ABC ~ △DEF

Example

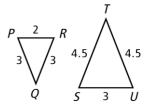
Explain why the triangles are similar and write a similarity statement.



Example

Verify that the triangles are similar.

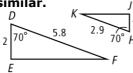
 \triangle *PQR* and \triangle *STU*



Example

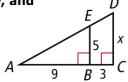
Verify that the triangles are similar.

 \triangle *DEF* and \triangle *HJK*



Example

Explain why $\triangle ABE \sim \triangle ACD$, and then find CD.



Properties

Properties of Similarity

Reflexive Property of Similarity

△ABC ~ △ABC (Reflex. Prop. of ~)

Symmetric Property of Similarity

If $\triangle ABC \sim \triangle DEF$, then $\triangle DEF \sim \triangle ABC$. (Sym. Prop. of \sim)

Transitive Property of Similarity

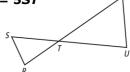
If $\triangle ABC \sim \triangle DEF$ and $\triangle DEF \sim \triangle XYZ$, then $\triangle ABC \sim \triangle XYZ$.

(Trans. Prop. of ~)

PROOFS!!

Given: 3UT = 5RT and 3VT = 5ST

Prove: $\triangle UVT \sim \triangle RST$



Example

The photo shows a gable roof. $\overline{AC} \mid \mid \overline{FG}$. $\triangle ABC \sim \triangle FBG$. Find \overline{BA} to the nearest tenth of a foot.



I Can

- ☐ Prove if triangles are similar with (AA, SSS and SAS)
- ☐ Use triangle similarity to solve problems